AP[®] CALCULUS AB 2010 SCORING GUIDELINES (Form B)

Question 5

Consider the differential equation $\frac{dy}{dx} = \frac{x+1}{y}$.

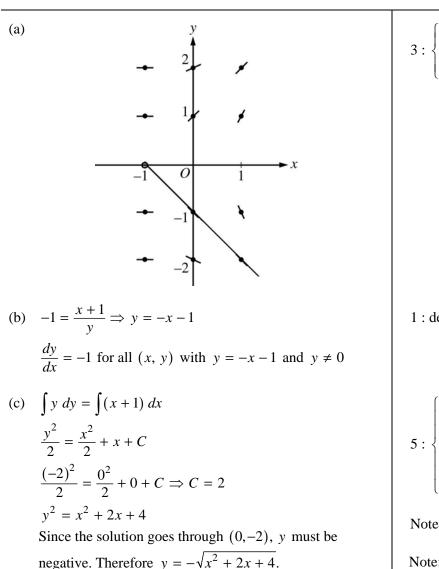
(a) On the axes provided, sketch a slope field for the given differential equation at the twelve points indicated, and for -1 < x < 1, sketch the solution curve that passes through the point (0, -1).

(Note: Use the axes provided in the exam booklet.)

(b) While the slope field in part (a) is drawn at only twelve points, it is defined at every point in the *xy*-plane for which $y \neq 0$. Describe all points in the *xy*-plane, $y \neq 0$, for

which
$$\frac{dy}{dx} = -1$$
.

(c) Find the particular solution y = f(x) to the given differential equation with the initial condition f(0) = -2.



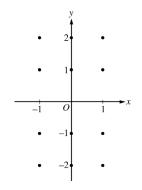
{ 1 : zero slopes
{ 1 : nonzero slopes
1 : solution curve through (0, -1)

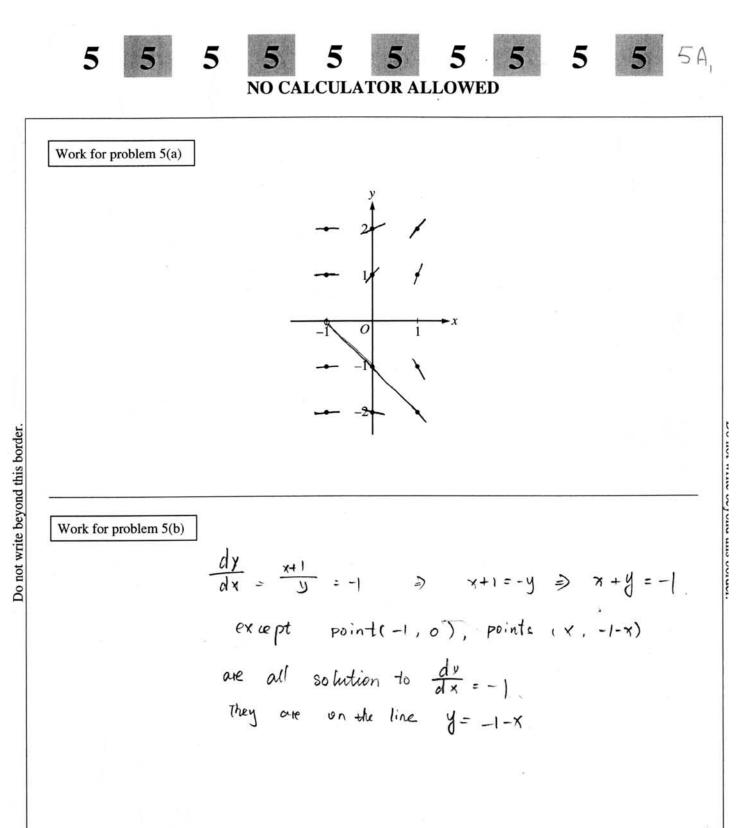
1 : description

(1 : separates variables
	1 : antiderivatives
5:{	1 : constant of integration
	1 : uses initial condition
	 separates variables antiderivatives constant of integration uses initial condition solves for <i>y</i>
Note: max 2/5 [1-1-0-0-0] if no	

Note: max 2/5 [1-1-0-0-0] if no constant of integration Note: 0/5 if no separation of variables

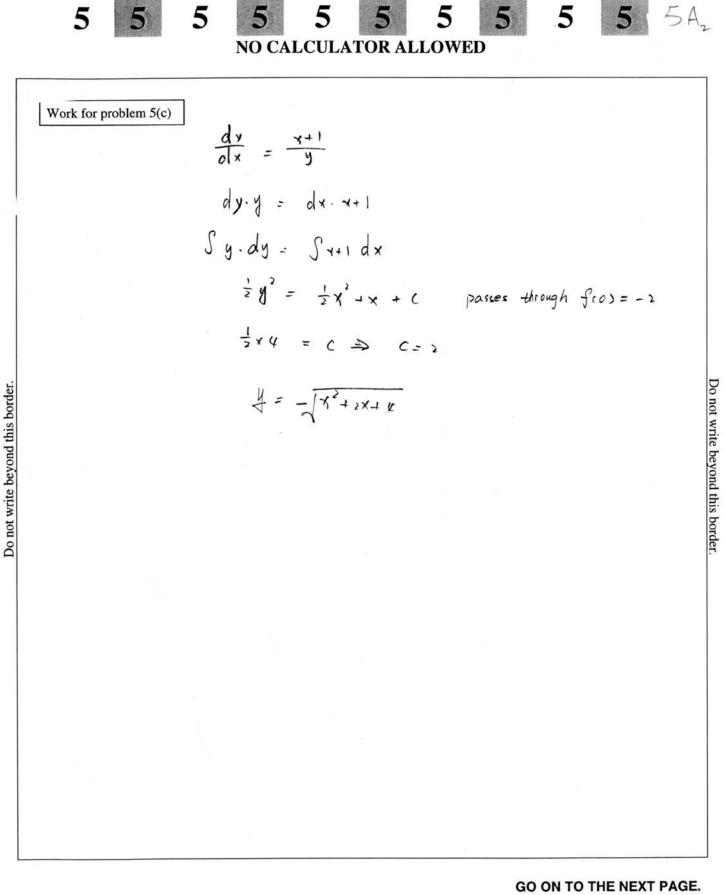


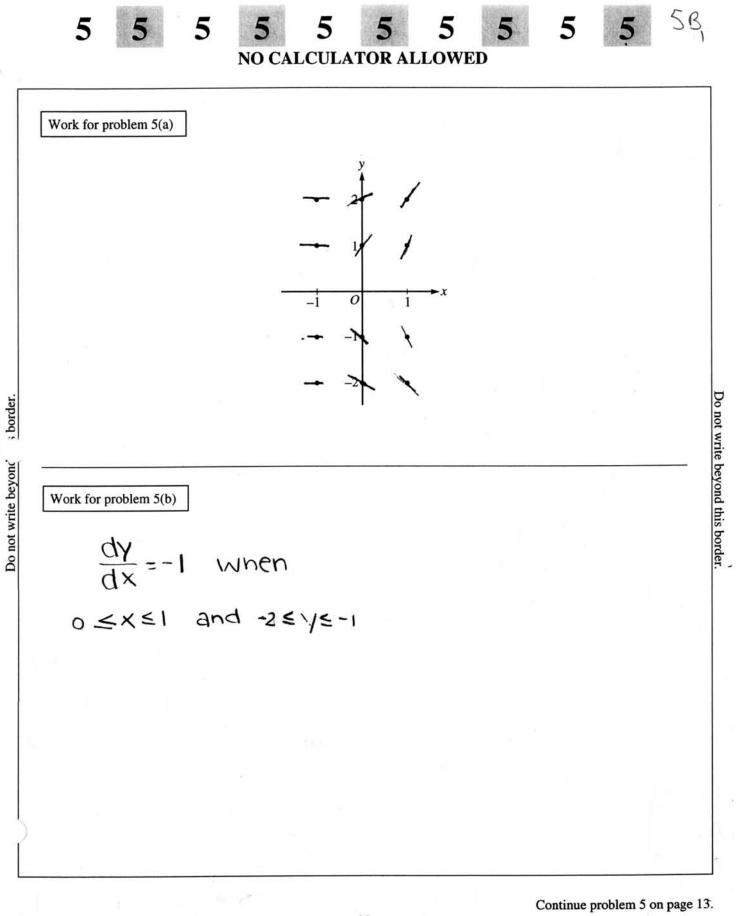




Continue problem 5 on page 13.

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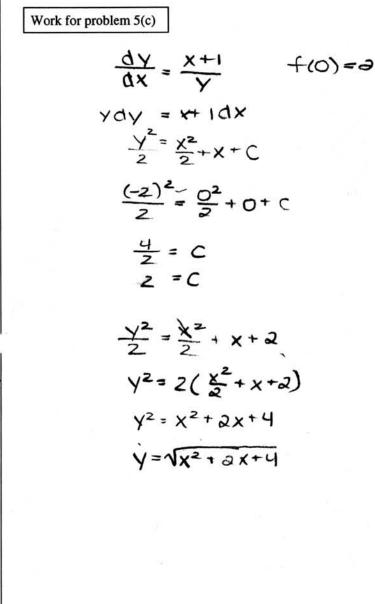


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NO CALCULATOR ALLOWED

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5B

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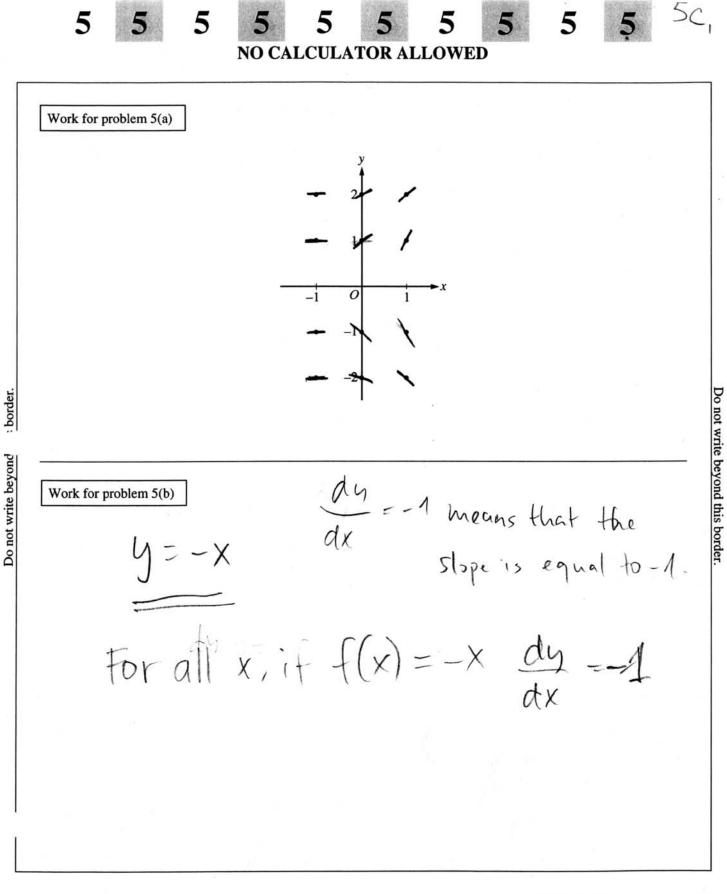
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Continue problem 5 on page 13.

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NO CALCULATOR ALLOWED Work for problem 5(c) f(0) = -2dy X+A dx = -2 dydx y.dy = dx (x+1) Zdy dx= $\int dx (x+\lambda)$ x= -24 .dy = y=XX1

5 5

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5C.

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AP[®] CALCULUS AB 2010 SCORING COMMENTARY (Form B)

Question 5

Sample: 5A Score: 9

The student earned all 9 points.

Sample: 5B Score: 6

The student earned 6 points: 2 points in part (a), no points in part (b), and 4 points in part (c). In part (a) the student's slope field is correct, but no solution curve is given. In part (b) the student's description is incorrect. In part (c) the student earned the first 4 points. Although the student uses the initial condition, the incorrect branch is chosen for the solution.

Sample: 5C Score: 3

The student earned 3 points: 2 points in part (a), no points in part (b), and 1 point in part (c). In part (a) the student's slope field is correct, but no solution curve is given. In part (b) the student's description is incorrect. In part (c) the student earned the point for separation of variables. The antiderivatives are not correct, so the student was not eligible for additional points.