

AP[®] Calculus BC

2003 Sample Student Responses

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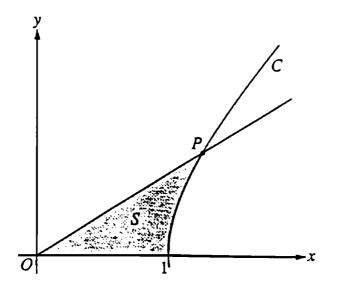
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Work for problem 3(a)

$$5/3 y = \sqrt{1+y^2}$$

 $y = .75$
 $x = 5/3 (.75)$
 $= 1.25$
P .75 a+ (1.25, .75)
 $dx/dy = 1/2 (1+y^2)^{-1/2} \cdot 2y$
 $dx/dy|_y = .75 = .6$
 $= \frac{y}{\sqrt{1+y^2}}$

Work for problem 3(b)

$$A = -\int_{0}^{.75} \frac{5}{3} y \, dy + \int_{0}^{.75} \frac{1}{5} \frac{1}{3} y \, dy$$

$$= \int_{0}^{.75} (\int_{1} \frac{1}{5} \frac{1}{3} - \frac{5}{3} \frac{1}{3} y) \, dy$$

$$\approx .347$$

Continue problem 3 on page 9.

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Work for problem 3(c) $x = r \cos \theta \quad y = r \sin \theta$ $x^{2} - y^{2} == 1$ $(r \cos \theta)^{2} - (r \sin \theta)^{2} = 1$ $r^{2} \cos^{2} \theta - r^{2} \sin^{2} \theta = 1$ $r^{2} (\cos^{2} \theta - \sin^{2} \theta) = 1$ $r^{2} = \frac{1}{\cos^{2} \theta - \sin^{2} \theta}$

Work for problem 3(d)

$$tun \theta = \frac{y}{x}$$

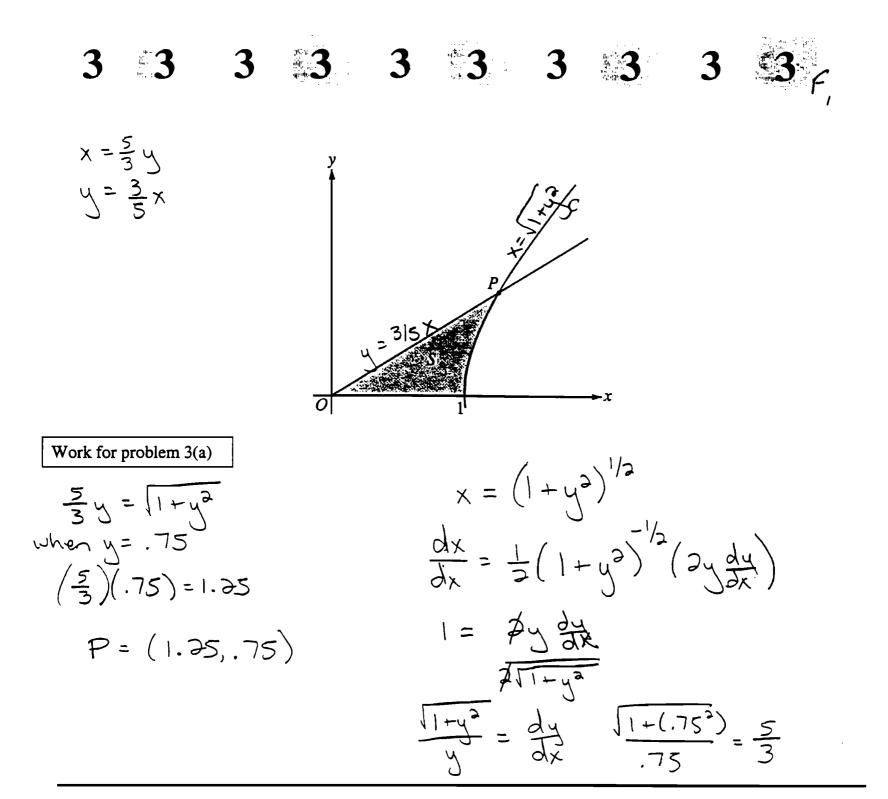
$$tun \theta = \frac{i75}{1.25}$$

$$\theta = \frac{.540}{.540}$$

$$A = \frac{1}{z} \int_{0}^{.540} \frac{d\theta}{\cos^{2}\theta - \sin^{2}\theta}$$

END OF PART A OF SECTION II

IF YOU FINISH BEFORE TIME IS CALLED, YOU MAY CHECK YOUR WORK ON PART A ONLY. DO NOT GO ON TO PART B UNTIL YOU ARE TOLD TO DO SO.



Work for problem 3(b)

$$\int_{0}^{.75} \left(\left(\sqrt{1+y^{2}} \right) - \left(\frac{5}{3} y \right) \right) dy = 5$$

$$S = .3460$$

Continue problem 3 on page 9.

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Work for problem 3(c) $y = r \sin 0$ $x = r \cos 0$ $y^{2} = r^{2} \sin^{2} 0$ $x^{2} = r^{2} \cos^{2} 6$

$$x^{2} - y^{2} = 1$$

$$r^{2}(\cos^{2}\theta - r^{2}\sin^{2}\theta) = 1$$

$$r^{2}(\cos^{2}\theta - \sin^{2}\theta) = 1$$

$$r^{2} = \frac{1}{\cos^{2}\theta - \sin^{2}\theta}$$

$$\frac{1}{2}\int_{0}^{1}\frac{1}{\cos^2\theta-\sin^2\theta}\,d\theta$$

END OF PART A OF SECTION II

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